

Nomenclature

Latin letters

a_i	activity of species i
a_{ki}	subscript to element k in molecular formula of species i
A	formula matrix: the $(M \times N)$ matrix whose entries are a_{ki}
A*	unit matrix or row-reduced echelon form of A
b_k	number of moles of element k
b	element-abundance vector with entries b_k
C	number of component species; number of linearly independent atom-balance equations
CRS	chemical reaction stoichiometry
F	number of degrees of freedom
F_s	number of stoichiometric degrees of freedom
G	Gibbs function
ΔG_j	change in Gibbs function for chemical equation j
ΔG_j^0	standard change in Gibbs function for chemical equation j
K_{aj}	equilibrium constant for chemical equation j
K_w	equilibrium constant for water dissociation
M	number of elements
MRM	matrix reduction method
n	species-abundance vector with entries n_i
n_i	number of moles of species i
δn_i	change in number of moles of species i
$\delta \mathbf{n}$	species-abundance-change vector with entries δn_i
N	number of species
N	stoichiometric matrix with elements ν_{ij}
N*	reduced stoichiometric matrix obtained from the matrix N
p	(protonic) charge
P	pressure
P^0	standard-state pressure
r	number of stoichiometric restrictions
R	maximum or proper number of linearly independent chemical equations
T	temperature (absolute)
X^0	standard-state composition

Greek letters

μ_i	chemical potential of species i
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$\mu_i^0(T, P^0, X^0)$	standard chemical potential of species i at the system T , the standard-state pressure P^0 , and the standard-state composition X^0
$\mu_i^0(T)$	standard chemical potential of species i at the system T (arguments P^0, X^0 are suppressed)
ν_i	stoichiometric coefficient of species i in a single chemical equation
ν_{ij}	stoichiometric coefficient of species i in chemical equation j
ν	stoichiometric vector with entries ν_i in a single chemical equation

Subscripts

i, j, k dummy indices

Other symbols

=	denotes chemical equation
\rightarrow	denotes irreversible chemical reaction
\rightleftharpoons	denotes reaction at equilibrium
T	as superscript, denotes transpose of a vector

Literature Cited

- [1] Anderson, G. M., and D. A. Crerar. *Thermodynamics in Geochemistry*. Oxford U. Press, Oxford, 1993.
- [2] Apse, J. I., and R. W. Missen. "Natural Equilibrium Distribution of Methane and the Deuteromethanes". *J. Chem. Educ.*, **44**:30, 1967.
- [3] Betz, M.L., J. P. Hupke, and D. W. Dickerhoof. "ChemBalance Wizard". <http://www.mines.edu/academic/chemistry/chembal/>, 1997.
- [4] Björnbom, P. H. *Ind. Eng. Chem., Fundam.*, **14**:102, 1975.
- [5] Björnbom, P. H. "letter to the editor concerning 'Some Remarks on the Calculation of Complex Chemical Equilibria by General Methods' by Smith". *Ind. Eng. Chem., Fundam.*, **17**:69, 1978.
- [6] Bottomley, J. "Note on a Method for Determining the Coefficients in Chemical Equations". *J. Chem. News J. Phys. Sci.*, **37**:110–111, 1878.

- [7] Brown, J.P., L. P. Brown, and R. M. Redd. "A Computer Program for Balancing Chemical Equations". *J. Chem. Educ.*, **49**:754, 1972.
- [8] Campanario, J. M. "Automatic 'Balancing' of Chemical Equations". *Computers Chem.*, **19**:85–90, 1995.
- [9] Carrano, S. A. "Balancing an Atypical Redox Equation". *J. Chem. Educ.*, **55**:382, 1978.
- [10] Cheluguet, E. L., R. W. Missen, and W. R. Smith. "Computer Calculation of Ionic Equilibria Using Species- or Reaction-Related Thermodynamic Data". *J. Phys. Chem.*, **91**:2428–2432, 1987.
- [11] Cobranchi, D.P., and E. M. Eyring. "Calculating Equilibrium Concentrations by the Continuation Method". *J. Chem. Educ.*, **68**:40–41, 1991.
- [12] Denbigh, K. G. *The Principles of Chemical Equilibrium*. Cambridge U. Press, 4th edition, 1981.
- [13] Ferguson, L. A. "How Do I Balance Thee?...Let Me Count the Ways". *J. Chem. Educ.*, **73**:1129, 1996.
- [14] Herndon, J. A. "On Balancing Chemical Equations: Past and Present". *J. Chem. Educ.*, **74**:1359–1362, 1997.
- [15] Jensen, W. B. "Unbalanced Chemical Equations" (letter to the editor). *J. Chem. Educ.*, **64**:646, 1987.
- [16] Kimura, R. T., Haunschild, P. A., and K. C. Lidell. *Metallurgical Trans.*, **15B**:213–219, 1984.
- [17] Kubachewski, O., and C. B. Alcock. *Metallurgical Thermochemistry*. Pergamon, New York, 5th edition, 1979.
- [18] Laidler, K. J., and M. T. H. Liu. *Proc. Roy. Soc.*, **A297**:365, 1967.
- [19] Madeley, W. D., and J. M. Toguri. "The Application of Free Energy Minimization Techniques to Determine Equilibrium Compositions in Systems of Metallurgical Interest". *Can. Metall. Quart.*, **12**:71–78, 1973.
- [20] McBride, L. E., and K. L. Adams. "The G. Frederick Smith Chemical Company". *J. Chem. Educ.*, **61**:625–626, 1984.

- [21] Missen, R. W. “Balancing Equations” (letter to the editor). *J. Chem. Educ.*, **47**:785, 1970.
- [22] Missen, R. W., and W. R. Smith. Letter to the editor concerning Olson(1997). *J. Chem. Educ.*, **75**:286, 1998.
- [23] Missen, R.W., and W. R. Smith. “A Question of Basic Chemical Literacy?”. *J. Chem. Educ.*, **66**:217–218, 1989. *erratum*, **66**:534.
- [24] Missen, R.W., and W. R. Smith. “The Permanganate-Peroxide Reaction: Illustration of a Stoichiometric Restriction”. *J. Chem. Educ.*, **67**:876–877, 1990.
- [25] Missen, R.W., C. A. Mims, and B. A. Saville. *Introduction to Chemical Reaction Engineering and Kinetics*. Wiley, New York, 1999. in press.
- [26] Noble, B. and J. W. Daniel. *Applied Linear Algebra*. Prentice-Hall, Englewood Cliffs, New Jersey, 2nd edition, 1977.
- [27] Nordstrom, D. K., and J. L. Munoz. *Geochemical Thermodynamics*. Blackwell Scientific Publications, Cambridge, MA, 2nd edition, 1994.
- [28] Olson, J. A. “An Analysis of the Algebraic Method for Balancing Chemical Reactions”. *J. Chem. Educ.*, **74**:538–542, 1997.
- [29] Porter, S. K. “How Should Equation Balancing Be Taught?”. *J. Chem. Educ.*, **62**:507–508, 1985.
- [30] Ramette, R. W. “REACT: Exploring Practical Thermodynamic and Equilibrium Calculations”. *J. Chem. Educ.: Software*, **8**(B1):13, 1995.
- [31] Rice, F. O., and K. F. Herzfeld. *J. Am. Chem. Soc.*, **56**:284, 1934.
- [32] Rosen, A. I. “A Computer Program Designed to Balance Inorganic Chemical Reactions”. *J. Chem. Educ.*, **54**:704, 1977.
- [33] Sanderson, R. V., and H. H. Y. Chien. “Simultaneous Chemical and Phase Equilibrium Calculations”. *Ind. Eng. Chem. Proc. Des. Dev.*, **12**:81–85, 1973.
- [34] Segraves, R. O., and D. Wickersham. “Learn Lessons from the PEPCON Explosions”. *Chem. Eng. Prog.*, **87**:65–69, June 1991.

- [35] Smith, W. R. “Some Remarks on the Calculation of Complex Chemical Equilibria by General Methods”. *Ind. Eng. Chem., Fundam.*, **15**:227–229, 1976.
- [36] Smith, W. R. “reply to letter to the editor by Björnbom concerning ‘Some Remarks on the Calculation of Complex Chemical Equilibria by General Methods’”. *Ind. Eng. Chem., Fundam.*, **17**:69–70, 1978.
- [37] Smith, W. R., and R. W. Missen. “What is Chemical Stoichiometry?”. *Chem. Eng. Educ.*, **13**:26–32, 1979.
- [38] Smith, W. R., and R. W. Missen. *Chemical Reaction Equilibrium Analysis: Theory and Algorithms*. Wiley-Interscience, New York, 1982. reprinted with corrections, Krieger, Malabar, FL., 1991.
- [39] Smith, W. R., and R. W. Missen. “Using Mathematica and Maple to Obtain Chemical Equations”. *J. Chem. Educ.*, **74**:1369–1371, 1997.
- [40] Spencer, N. D., and C. J. Pereira. “Partial Oxidation of CH₄ to HCHO over a Mo₃-SiO₂ Catalyst: A Kinetic Study”. *AICHE J.*, **33**:1808–1812, 1987.
- [41] Stout, R. “Redox Challenges”. *J. Chem. Educ.*, **72**:1125, 1995.
- [42] Swinnerton, J. W., and W. W. Miller. “Use of a Digital Computer for Solving a Complex Chemical Equilibrium”. *J. Chem. Educ.*, **36**:485–489, 1959.
- [43] Vaidyanathan, K., and L. K. Doraiswamy. “Controlling Mechanisms in Benzene Oxidation”. *Chem. Eng. Sci.*, **23**:537–550, June 1968.
- [44] E. Weltin. “Let a Computer Balance Your Chemical Equations and Determine the Number of Independent Reactions”. *J. Chem. Educ.*, **71**:295–297, 1994.
- [45] D. J. Wink. “The Use of Matrix Inversion in Spreadsheet Programs to Obtain Chemical Equations”. *J. Chem. Educ.*, **71**:490–492, 1994.

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